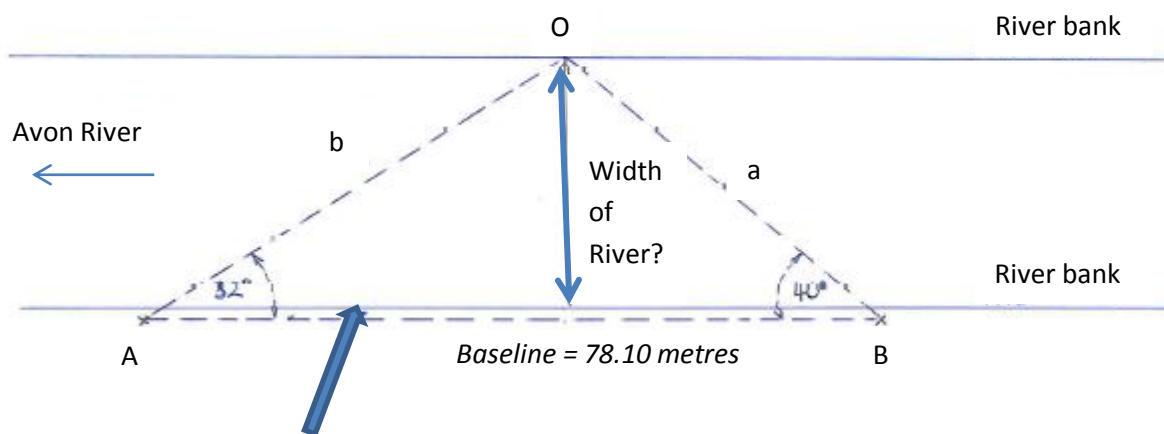


Surveying - Answers		Curriculum Area: Mathematics and Statistics, Level 5-6	Strand: Geometry and Measurement
Achievement Objectives:	Apply trigonometric ratios and Pythagoras' theorem in two dimensions		
Learning Intention:	Apply laws of trigonometry to find the location of a set point		

A surveyor marks 2 positions on one side of the Avon River, a metre off the bank, measures 78.10 metres between them, then sets up a theodolite at each position and measures the angles at A & B to O.

Question; What is the width of the of the Avon River at Point O?



Baseline is 1 metre off the river bank

Angle A = 32 degrees

Angle B = 40 degrees

[Use the sine rule to find the unknown sides of the triangle]

Show your working here:

Answer

• Angle at opposite bank is $180^\circ - 32^\circ - 40^\circ = 108^\circ$.

• Using sine rule, unknown sides of triangle are: $\frac{78.10}{\sin 108^\circ} = \frac{a}{\sin 32^\circ} = \frac{b}{\sin 40^\circ}$

$$a = \sin 32^\circ \times \frac{78.10}{\sin 108^\circ} = 43.52\text{m}$$

$$b = \sin 40^\circ \times \frac{78.10}{\sin 108^\circ} = 52.79\text{m}$$

• Perpendicular distance from baseline to opposite bank = $52.79 \times \sin 32^\circ = 27.97$
or $43.52 \times \sin 40^\circ = 27.97$

• Width of river is $27.97 - 1 = \underline{\underline{26.97 \text{ metres}}}$